

# Scheduling Parametric Data Flow Graphs

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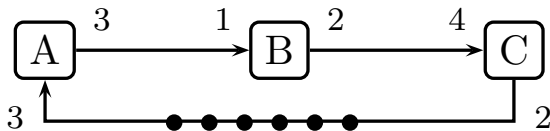
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Pascal Fradet (INRIA)  
Bruno Lavigueur (STMircoelectronics)

## Scheduling parametric data flow applications on many core platforms

- Data flow
  - ▶ Data flow models
  - ▶ Data flow scheduling
- Scheduling framework
  - ▶ Scheduling model - STHORM platform (ex. P2012)
  - ▶ Scheduling framework

- 1 Data Flow Models
  - Synchronous Data Flow
  - Parametric Data Flow
- 2 Scheduling

# SDF - Synchronous Data Flow



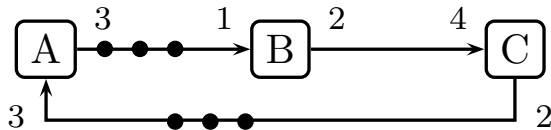
A Synchronous Data Flow graph

- **Actors** ( $A, B, C$ ) & **edges** ( $AB, BC, CA$ )  
Function units & Communication links (FIFOs)
- **Port rates:**  
Number of tokens transferred through a port
- **Graph State:**  $S_i = [0 \ 0 \ 6]$   
Number of tokens on the graph's edges

**SDF<sup>1</sup>:** Port rates are fixed and known at compile time

<sup>1</sup>Lee and Messerschmitt 1987

# SDF - Synchronous Data Flow



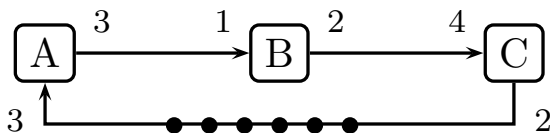
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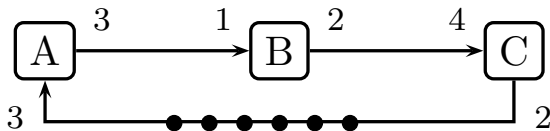
# SDF - Analysis



A Synchronous Data Flow graph

- **Actor solutions** ( $\#A, \#B, \#C$ ) & **repetition vector** ( $r$ ) :  
 $\#A = 2, \#B = 6, \#C = 3 \Rightarrow r = [2 \ 6 \ 3]$
- **Iteration**: Sequence of firings that return the graph to  $S_i$
- **Schedule**: Execution of a complete iteration e.g.  $A^2; B^6; C^3$
- **Liveness**: Enough initial tokens on each directed cycle

# SDF - Scheduling



A Synchronous Data Flow graph

- Repetition vector:  $[2 \ 6 \ 3]$

- Sequential schedules:

- ▶  $A^2; B^6; C^3$
- ▶  $A; B^2; C; B; A; B; C; B^2; C$

- Single appearance schedule
- Minimum buffer size schedule

- Parallel schedules:

- ▶  $A; (A \parallel B); [B; (B \parallel C)]^2; B; C$  - As Soon As Possible schedule (ASAP)

# SDF - Advantages & Disadvantages

## Advantages

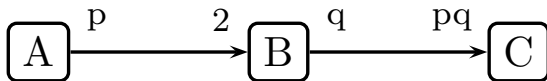
- + Modular and reusable design, suitable for DSP
- + Parallelism Exposure
- + Boundedness and liveness guaranteed at compile time
- + Static scheduling - Timing guaranteed

## Disadvantages

- Too restrictive to express more advanced applications  
(e.g. video codec applications)



# PDF - Parametric Data Flow



A parametric data flow graph

- Simplified version of SPDF <sup>2</sup> and PSDF <sup>3</sup> models
- Parameters change between iterations
- Symbolic analysis of the graph

Repetition vector:  $\begin{bmatrix} 2 & p & 1 \end{bmatrix}$

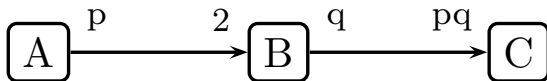
**PDF:** Parametric port rates that change between iterations

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<sup>2</sup>P.Fradet et al. 2012

<sup>3</sup>B.Bhattacharya and S.Bhattacharyya 2001

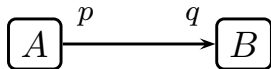
# PDF - Scheduling



A parametric data flow graph

- Repetition vector:  $[2 \ p \ 1]$
- Sequential schedules:
  - ▶  $A^2; B^p; C$  - Single appearance schedule
- Parallel schedules:
  - ▶ Difficult to express ASAP schedule

# PDF - ASAP scheduling



A PDF edge

- Case  $p \geq q$  :
  - ▶  $A; (A|B)^{q-1}; B^{p-q+1}$
- Case  $q > p$  :
  - ▶ Subcase  $q = kp$  :
    - $A; (A^{k-1}; (A|B))^{p-1}; A^{k-1}; B$
  - ▶ Subcase  $q = kp + r, 0 < r < p$  :
    - Needs iterative comparison of the values of  $p$  and  $q$

# PDF - Advantages & Disadvantages

## Advantages

- + Modular and reusable design, suitable for streaming applications
- + Parallelism Exposure
- + Boundedness and liveness guaranteed at compile time
- + Increased expressiveness

## Disadvantages

- (Quasi -) static parallel scheduling possible is more involved  
(e.g. ASAP scheduling is a challenge)

## 1 Data Flow Models

## 2 Scheduling

- STHORM platform
- Scheduling framework
- Future Work

# STHORM platform

## Platform Features

- Many - core platform designed by **STMicroelectronics**
- 1-32 clusters with 1-16 cores:
  - ▶ Software cores: General Purpose Processors (GPP)
  - ▶ Hardware cores: HardWare Processing Elements (HWPE)

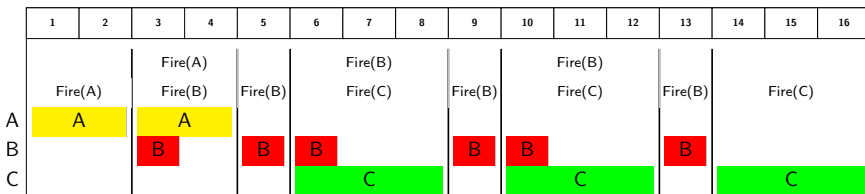
## Mapping assumptions

- Application fits in a **single cluster**
- Each actor is executed by a **GPP** or implemented as a **HWPE**
- The schedule is executed by a **GPP**

# Slotted scheduling model

- Compatible with the scheduling model of STHORM
- Uses a slot notion like in blocked scheduling <sup>4</sup>
  - + Actors synchronize after each execution
  - + Reduces complexity of parallel scheduling
  - + Compatible with other parallel programming models (CUDA, OpenGL)
  - May introduce slack

Repetition vector:  $[2 \ 6 \ 3]$



<sup>4</sup>S.Ha et al. 1991

# Scheduling framework features

## The framework should

- Automatically produce **ASAP** schedules
- Be **expressive** and **flexible** for different
  - ▶ Platforms
  - ▶ Optimization criteria
  - ▶ Scheduling strategies

**Main idea:** Production of different schedules with the same (ASAP) algorithm



# Scheduling framework overview

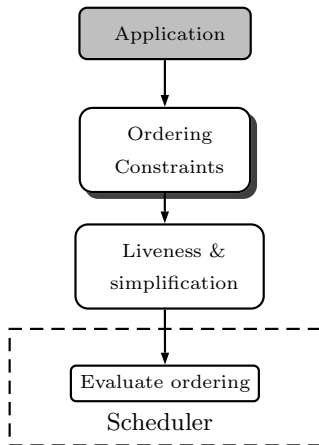


Figure : Scheduling framework

# Scheduling framework overview

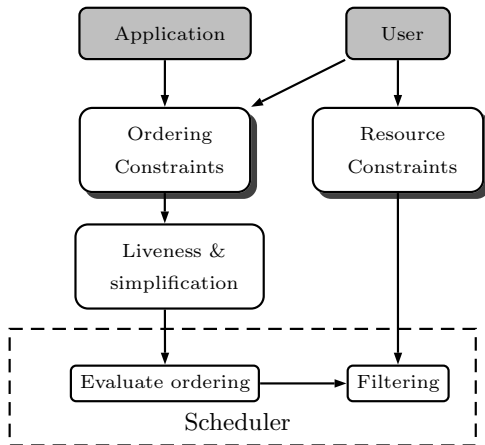


Figure : Scheduling framework

# Scheduling constraints

- **Ordering Constraints:** Express the partial ordering of the firings

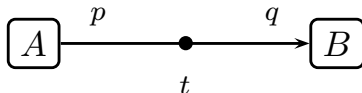
$$X_i > Y_{f(i)}$$

- **Resource Constraints:** Control the parallel execution

**replace  $S_A$  by  $S_B$  if *condition***

where  $S_B \subseteq S_A$  and  $S_B \neq \emptyset$

# Constraint Examples



**Graph Constraint:** Data dependency

$$B_i > A_{f(i)} \quad \text{with} \quad f(i) = \left\lceil \frac{q \cdot i - t}{p} \right\rceil$$

**User Constraint:** Buffer capacity restriction to  $k$

$$A_i > B_{g(i)} \quad \text{with} \quad g(i) = \left\lceil \frac{p \cdot i + t - k}{q} \right\rceil$$

**Resource Constraint:** Mutual exclusion of A and B

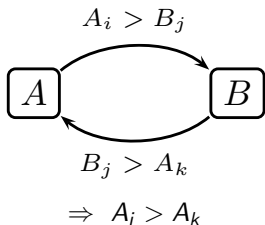
**replace  $\{A, B\}$  by  $\{A\}$**

# Constraint deadlock Detection

## Deadlock

A set of ordering constraints deadlocks when it implies (by transitivity) a constraint of the form:

$$\exists A, i, j, (A_i > A_j) \wedge (i \leq j)$$



$\forall$  cycle  $A_i > A_k$   
check if  $i > k$

# Deadlock detection example

Constraints:

$$B_i > A_{f(i)}$$

$$A_i > B_{g(i)}$$

Cycle:

$$A_i > A_{f(g(i))}$$

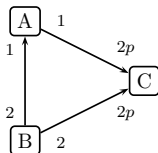
Deadlock free condition:

$$i > f(g(i))$$

Solution:

$$\begin{aligned}
 i > f(g(i)) &\Leftrightarrow i > \left\lceil \frac{q \cdot \left\lceil \frac{p \cdot i - k}{q} \right\rceil}{p} \right\rceil \\
 &\Leftrightarrow i > \frac{q \cdot \left( \frac{p \cdot i - k}{q} + 1 \right)}{p} + 1 \\
 &\Leftrightarrow i > i + \frac{q - k}{p} + 1 \\
 &\Leftrightarrow k > p + q \\
 &\Leftrightarrow k > p_{\max} + q_{\max}
 \end{aligned}$$

# Constraint simplification



## Constraints:

$$A_i > B_{\lceil \frac{i}{2} \rceil}$$

$$C_i > B_{\lceil \frac{2pi}{2} \rceil}$$

$$C_i > A_{pi}$$

## Firing Function:

$$B_i = i, \quad i \in [1 \cdots p]$$

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$$A_i = \max(B_{\lceil \frac{i}{2} \rceil}, A_{i-1}) + 1, \quad i \in [1 \cdots 2p]$$

$$\Rightarrow A_i = 2i + 1$$

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$$C_i = \max(B_{pi}, A_{pi}, C_{i-1}) + 1, \quad i = 1$$

$$\Rightarrow C_i = \max(A_{pi}, C_{i-1}) + 1$$

$$\Rightarrow C_i = 2p + 1$$

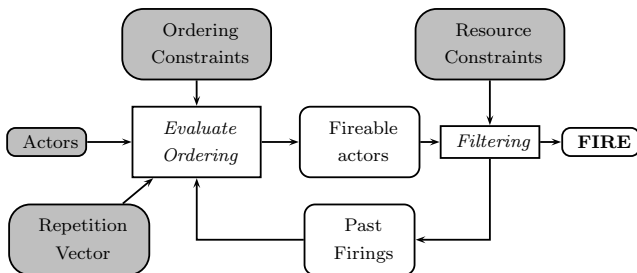
## Schedules:

$$B : \mathcal{F}^p$$

$$A : \mathcal{E}; (\mathcal{E}; \mathcal{F})^{2p}$$

$$C : \mathcal{E}^{2p}; \mathcal{F}$$

# Run-time scheduler



Overall small overhead:

- Concurrent execution with actors
- Coarse - grain graph
- Optimization of static parts of the graph



# Conclusions

We presented a **scheduling framework for PDF** applications that:

- **Flexible** constraint framework for PDF graphs:
- **Modular** way to adjust the schedule
- **Expressive** power to optimize the schedule
- **Automatically** generates of ASAP schedules
- **Statically guarantees** boundness and liveness of the schedule

## On-going work

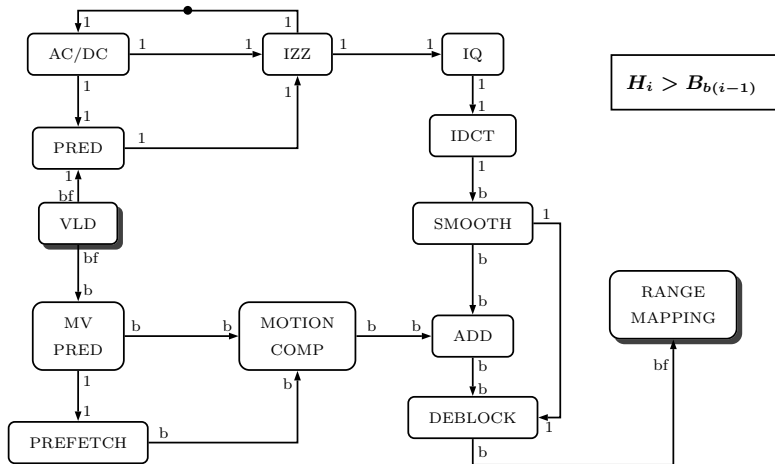
- **Implementation and integration** within **ST**'s SDK
- **Evaluation of the scheduler** with real world applications

## Future work

- **Introduction of timing information**
- **Flexible slotted scheduling model** already used on the platform

Thank you for your attention!

# Use case example: VC1 decoder



VC-1 capture in PDF

# Resource constraint examples

- Mutual Exclusion (A and B: specific actors )

**replace** A, B **by** A

- Bounded Parallelism (x,y,z: variables - can be any actor)

**replace** x, y, z **by** x, y

- Timing optimization

**replace** x, y **by** x **if**  $short(x) \wedge long(y)$

- Power optimization

**replace** x, y **by** x **if**  $high(x) \wedge high(y)$

**replace** x, y, z **by** x, y **if**  $high(x) \wedge low(y) \wedge low(z)$